Inertially confined fusion plasmas dominated by alpha-particle self-heating

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Alpha-particle self-heating, the process of deuterium–tritium fusion reaction products depositing their kinetic energy locally within a fusion reaction region and thus increasing the temperature in the reacting region, is essential for achieving ignition in a fusion system. Here, we report new inertial confinement fusion experiments where the alpha-particle heating of the plasma is dominant with the fusion yield produced exceeding the fusion yield from the work done on the fuel (pressure times volume change) by a factor of two or more. These experiments have achieved the highest yield (26 ± 0.5 kJ) and stagnation pressures (≈220 ± 40 Gbar) of any facility-based inertial confinement fusion experiments, although they are still short of the pressures required for ignition on the National Ignition Facility (~300–400 Gbar). These experiments put us in a new part of parameter space that has not been extensively studied so far because it lies between the no-alpha-particle-deposition regime and ignition.

Previously, we reported on experiments on inertial confinement fusion experiments (ICF1) at the US National Ignition Facility (NIF2) where the fusion energy produced was greater than the amount of energy deposited into the fusion fuel (fuel gain > 1). Here, we discuss new results4−6 using a simple dynamic model of the hotspot to gain insight into the data. We find that our highest performing experiments sit close to the point where energy deposition from alpha heating is nearly balanced by radiation losses of the hotspot to gain insight into the data. We find that our

\[
\frac{d}{dt} (e m_{\text{halt}} R) = 4\pi R^2 P_{\text{lu}} \tag{1}
\]

As the pressure in the centre of the implosion—the ‘hotspot’ pressure $P_{\text{lu}} = 0.77 \rho_0 T_{\text{lu}}$ (in gigabar, g cm$^{-1}$, kiloelectronvolt units)—increases, both the hotspot density, $\rho_0$, and thermal temperature, $T_{\text{lu}}$, rise. At this point in time the NIF laser has delivered its full laser pulse and the ablation pressure external to the implosion becomes negligible in comparison with the central pressure. At the moment the deceleration of the implosion begins, a shock wave transits outward from the inner surface of the fuel to the outer surface. As the DT fuel is compressible, this effectively means the full inertia of the DT fuel and remaining ablator does not act on the hotspot, but only on the shocked fraction of the fuel, hence the

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Figure 1 | Hotspot pressure versus coasting time (implosion speed). A schematic of a NIF implosion near peak-compression is round (upper left) ideally, with a dense shell (blue) of compressed DT fuel and remaining ablation material surrounding a much lower density (red) hotspot. As the ‘coast time’ is reduced, by extending the laser pulse, the implosion speed increases, and the hotspot pressure should rapidly increase according to ideal implosion models (lower right, red curve). The coast time (lower left) equals the implosion bang time minus the time the laser is turned off and is empirically related to implosion speed (best fit: \( v_{\text{imp}} = 394.11 - 75.9t_{\text{coast}} \)). Although implosion data from NIF do show an increase in hotspot pressure as implosion speed increases (lower right, blue data points), the rate of increase is much less than ideal. In reality, implosions may not have the ideal 1D geometry, but instead may have highly modulated 3D shell and hotspot geometries (upper middle). Thin spots of low areal density in the shell would provide little inertial confinement and would allow a path for hotspot energy and mass loss (upper right) that would not occur in the ideal implosion case. Including the effects of a lossy implosion is consistent with the NIF data (lower right; cyan curve). The model that produced the cyan curve assumes \( Q_{\text{cond}} \approx \nu^4 \) (scaling expected from Rayleigh-Taylor-like growth). The purple dashed curve is a power-law best fit to the data that shows \( P_{\text{hs}} \sim v^{2.73} \). Here, the \( P_{\text{stag}} \) data are those inferred from the measured \( T_{\text{sv}}(\text{DT}) \). All error bars, \( \pm \sigma \).

efficiency factor, \( \epsilon \approx 1 \). Poor implosion symmetry (that is, time-dependent shape) or break-up of the imploding shell can also effectively lower \( \epsilon \) when applying equation (1) to an implosion experiment. Generally in ICF implosions on NIF, because of the high densities and pressures achieved, inter particle collisions force the ion and electron temperatures to be approximately equal in the fusion plasma: \( T_{\text{ion}} \approx T_{\text{e}} \), so we generally just refer to \( T_{\text{hs}} \) here. The infalling shell of DT fuel does mechanical PdV (pressure times volume change) work on the lower density hotspot, increasing the hotspot internal energy and therefore temperature according to

\[
\frac{dT_{\text{hs}}}{dt} = Q_{\text{dt}} - Q_{\text{bc}} - Q_{\text{cond}} - \frac{4\pi R^2 P_{\text{hs}} R}{m_{\text{hs}}} - \left( \rho_{\text{hs}} v_{\text{hs}}^3 + 3P_{\text{hs}} v_{\text{cs}} \right) \cdot A_{\text{hs}}
\]

(2)

where the DT heat capacity is \( c_{\text{DT}} = 0.115 \text{GJ g}^{-1} \text{ keV}^{-1} \), \( Q_{\text{bc}} = 3.1 \times 10^7 \rho_{\text{hs}} \sqrt{T_{\text{hs}}} \) (GJ g\(^{-1}\) s\(^{-1}\)) is the specific cooling power of bremsstrahlung X-rays in the optically thin limit (see Methods), and \( Q_{\text{cond}} = 5.384 \times 10^{11} / (\rho_{\text{hs}}^{0.86} R_{\text{hs}}^{3}) \) (GJ g\(^{-1}\) s\(^{-1}\)) is a modern version of the Spitzer–Harm electron heat conduction model \( (Q_{\text{cond}} = 5.9 \times 10^7 T_{\text{hs}}^{3/2} / (\rho_{\text{hs}} R_{\text{hs}}^2) \) in GJ g\(^{-1}\) s\(^{-1}\)) based on the Sesame \(^{10} \) equations of state. The alpha-particle self-heating contribution to the hotspot specific power, \( Q_{\alpha} = 8.18 \times 10^5 \rho_{\text{hs}} f_{\alpha}(\sigma v) \) (GJ g\(^{-1}\) s\(^{-1}\)), depends on the DT fusion reaction rate \( (\sigma v) \approx 2.68 \times 10^{-20} T_{\text{hs}}^{3.9} \text{cm}^3 \text{ s}^{-1} \) (in the range of 3 keV < \( T_{\text{hs}} < 5 \text{ keV} \) relevant to the experiments discussed herein—see Methods) and the fraction, \( f_{\alpha} \), of alpha-particles stopped inside the hotspot\(^{11} \) where

\[
f_{\alpha} = 1 - \frac{1}{4[(\rho r)_{hs}/\rho \lambda_c] + 160[(\rho r)_{hs}/\rho \lambda_c]^{3/4}}
\]

(3)

where the alpha-particle stopping range can be found from

\[
\rho \lambda_c = \frac{0.025T_{\text{hs}}^{3/4}}{1 + 0.0082(T_{\text{hs}}^{5/4})}
\]

(4)
in centimetre, gram, kiloelectronvolt units.

The last term in equation (2) represents, in our simplified picture (upper right-hand side of Fig. 1), the total kinetic plus internal.
energy lost from the hotspot by ejecting hotspot mass through one or more weak spots or perforations (collectively of cross-sectional area \(A_{\text{leak}}\), which defines a dimensionless ‘defect’, \(D = A_{\text{leak}}/4\pi R^2\)) in the shell. Non-uniformities in the implosion grow owing to unstable growth in convergence and create variations in shell areal density, \((\rho R)_{\text{leak}}\) (see Fig. 1) that, if extreme enough, essentially provide little to no inertial confinement of the hotspot—this is what \(D\) is meant to represent. Time-dependent asymmetries in the hohlraum-generated X-ray bath\(^{12,13}\) that drive the ablation pressure of the capsule are implicated. Perforations in the shell could additionally be produced by growth of baroclinic vorticity seeded by engineering features such as capsule fill tubes (the \(\sim 10 - 15\) \(\mu\)m-diameter glass tube that is used to fill the capsule with DT) or mounting membranes (‘tents’ that are diaphragms of \(\sim 15-45\) nm thickness plastic that hold the capsule in the centre of the hohlraum). The velocity, \(V_{\text{esc}} = \sqrt{2H_m/m_{\text{fuel}}}\) of mass and energy outflow through a weak spot in the shell is given by the stagnation enthalpy, \(H_m = E_{\text{kin}} + P_{\text{leak}} V_{\text{esc}}^2\), at the centre of the implosion because the enthalpy outside the shell is small in proportion to the ablation pressure (hundreds of megarbar) being small compared with an ICF implosions central pressure (hundreds of gigabar).

The ideal boundary between an un-ignited and ignited fusion state is given by the right-hand side of equation (2) with \(\hat{R} = 0\) and \(A_{\text{leak}} = 0\), consistent with the condition of Lawson\(^{8,14}\). That is, when in the absence of external heating, the power from alphaparticle self-heating outstrips the losses of power from radiation and electron conduction \((Q_e > Q_{\text{brems}} + Q_{\text{cond}})\), the plasma temperature rapidly increases in an explosive manner. The nearly hyperbolic boundary defined by \(Q_e = Q_{\text{brems}} + Q_{\text{cond}}\) (see Fig. 2, bottom frames) depends solely on \(T_m\) and the areal density of the hotspot, \((\rho R)_{\text{hotspot}}\) (ref. 8), so showing our implosion experiment data in the space of these two parameters is the most appropriate metric for gauging how far from ignition our results are at present (yield is not a useful metric for gauging proximity to ignition because ignition is a threshold process).

Following from equations (3)–(4) \(\sim 70\%\) of the fusion alphas are stopped in the hotspot for our implosion. The alpha-particles created during the period of DT fusion that do not stop in the hotspot are stopped in the inner surface of the much denser compressed DT fuel shell, depositing their energy there. Electrons carrying heat outward from the hotspot similarly stop in the inner surface of the DT fuel shell and also deposit their energy. The
deposition of energy into DT fuel causes it to ablate inwards and add DT mass to the hotspot\(^{15,16}\) (and return the energy that was deposited into the fuel to the hotspot) as the hotspot heats, according to the expression

\[
dm_{hs}/dt = \frac{m_{hs}}{0.115T} \left[ Q_o \left( \frac{1 - f_o}{f_a} \right) + Q_{\text{cond}} \right] - \rho_{hs} v_{hs} A_{\text{leak}}
\]

where the last term represents the hotspot mass loss due to the flow of hotspot material driven out through a weak spot/perforation in the shell as the internal hotspot pressure rises (see Fig. 1). As the hotspot mass, density and temperature evolve in time, the fusion yield rate can be calculated from \(dY/dt = 5.0 \times 10^{-5} \times m_{hs}Q_{o}/f_a\) in kilojoule units, where the factor of 5 comes from the fact that only 20% of the total DT fusion yield comes from alpha-particles (the other 80% coming from neutrons). Although not immediately obvious, combining equations (2) and (5), using the fact that the hotspot internal energy is \(E_{hs} = 0.115m_{hs}T_{hs} = 3/2P_{hs}V_{hs}\) (where \(V_{hs} = 4\pi R_{hs}^2\)) the one obtains an equation (like ref. 17) for hotspot pressure evolution,

\[
P_{hs} + 5P_{hs}^2 = \frac{P_{hs}}{R} \left( \frac{1}{f_a} Q_o - Q_{\text{frem}} - Q_{\text{leak}} \right) - \rho_{hs} v_{hs} A_{\text{leak}}
\]

where \(Q_{\text{leak}} = A_{\text{leak}}(\rho_{hs} v_{hs} + 3P_{hs}v_{hs})/(2m_{hs})\) is the cooling of the hotspot due to energy loss through a perforation in the imploding shell with the last term in the equation being the effect of hotspot mass loss though the shell perforation. In ref. 17, the loss terms in equation (6) are not present and the fusion reaction rate is assumed to scale differently. The non-ideal effect in equation (6), a perforated implosion, is conceptually different from the non-ideal effect of Rayleigh–Taylor instability–driven spikes reducing the effective hotspot size\(^{48}\). When the right-hand side of equation (6) is negligible, adiabatic compression, \(P_{hs}R^2 = \text{constant}\), is recovered (see the Methods). Note that when \(Q_o = f_oQ_{\text{frem}}\) in equation (6), \(T = 4.3\) keV, which is the classic textbook ‘ignition temperature’\(^{49}\) and is a representative burn-averaged temperature of many of our high-foot implosions.

This dynamic model, equations (1)–(5), or equivalently equations (1), (2) and (6), can be constrained to implosion time-integrated data to form a picture of the dynamics around the time of peak X-ray and neutron emission (‘bang time’). It also unfolds the degree of alpha-particle self-heating over the duration of the fusion burn, which is the primary purpose of the above development. When constrained to a series of high-foot experiments on the NIF where the implosion speed is increased by keeping the laser drive on longer into the implosion as measured by a reduction in the ‘coast time’, the time between bang time and the time the laser is shut off, the model with shell perforations seems to capture the pressure data trend (Fig. 1). The data scaling shows that \(P_{\text{eig}} \sim v^{4.75}\) until a peak of ~220 Gbar, but then declines.

As seen in Fig. 2, as our implosion experiments have progressed to higher temperatures and hotspot areal densities as a result of being driven with successively higher amounts of laser energy and therefore fuel kinetic energy, the different interpretations of \((\rho R_{hs})_0\) and \(T_{hs}\) differ outside of standard error bars. For these same implosions, shell areal density variations as inferred from neutron activation diagnostics\(^{29,30}\) show more variation (for example, Fig. 2). For the most compressed implosions shell areal density variations are estimated to be as large as ~50%. Experiments driven with relatively low laser energies of 1.3–1.5 MJ occupy the region around \(T_{hs} \sim 3\) keV and \((\rho R_{hs})_0 \sim 0.1\) g cm\(^{-2}\), and do not show differences in temperature inference even though X-ray and neutron imaging of these experiments showed non-ideal (for example, toroidal) shape\(^{20–22}\) at the time of peak X-ray and neutron brightness.

For ICF implosions neither \(T_{hs}\) nor \((\rho R_{hs})_0\) is measured directly, they are instead inferred from other diagnostic data. Hotspot areal density, \((\rho R_{hs})_0\), is inferred\(^{23,24}\) from a combination of data coming from the fusion yield measurement\(^{25,26}\), a temporal measurement of the fusion burn duration, imaging data from X-ray emission\(^{27,28}\), imaging data from neutron emission\(^{29,30}\), and the ion temperature. Burn- and volume-averaged ion temperature quantities \((T_{\text{ion}})\) are directly related to the temporal spread, full-width at half-maximum, of the neutron-time-of-flight (NToF) detector\(^{31}\) signals using simple formulae\(^{32}\). As DT fusion neutrons, with peak energy around 14.1 MeV, travel faster and are scattered less than DD fusion neutrons, with peak energy around 2.5 MeV, the NToF detector can be used to obtain two temperature measurements of the fusion regions they sample—a \(T_{\text{ion}}(\text{DT})\) and \(T_{\text{ion}}(\text{DD})\). Ideally, \(T_{\text{ion}}(\text{DT}) \approx T_{\text{ion}}(\text{DD})\), which simplifies the data interpretation, but even for an ideal one-dimensional (1D) ICF implosion \(T_{\text{ion}}(\text{DT})\) will exceed \(T_{\text{ion}}(\text{DD})\) by ~200–300 eV owing to the electron-

### Table 1 | Table of input and derived yield amplification metrics.

<table>
<thead>
<tr>
<th>Shot</th>
<th>(E_{\text{laser}}) (MJ) absorbed</th>
<th>(m_{abl}) ((\mu)g)</th>
<th>(m_{abl}) ((\mu)g)</th>
<th>(Y_o/Y_{\text{no-}\alpha}) (dm)</th>
<th>(Y_o/Y_{\text{no-}\alpha})</th>
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<tbody>
<tr>
<td>N130501</td>
<td>1.1 ± 0.022</td>
<td>2.735</td>
<td>177</td>
<td>1.23 ± 0.041</td>
<td>1.19 ± 0.02</td>
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<tr>
<td>N130530</td>
<td>1.26 ± 0.025</td>
<td>2.819</td>
<td>179</td>
<td>1.16 ± 0.029</td>
<td>1.14 ± 0.01</td>
</tr>
<tr>
<td>N130710</td>
<td>1.28 ± 0.026</td>
<td>2.818</td>
<td>182</td>
<td>1.3 ± 0.054</td>
<td>1.25 ± 0.03</td>
</tr>
<tr>
<td>N130802</td>
<td>1.29 ± 0.026</td>
<td>2.738</td>
<td>177</td>
<td>1.16 ± 0.029</td>
<td>1.14 ± 0.02</td>
</tr>
<tr>
<td>N130812</td>
<td>1.44 ± 0.029</td>
<td>2.781</td>
<td>179</td>
<td>1.4 ± 0.072</td>
<td>1.53 ± 0.06</td>
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<tr>
<td>N130927</td>
<td>1.63 ± 0.033</td>
<td>2.784</td>
<td>185</td>
<td>1.69 ± 0.12</td>
<td>1.64 ± 0.07</td>
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<tr>
<td>N131119</td>
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<td>179</td>
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<td>179</td>
<td>1.8 ± 0.14</td>
<td>2.08 ± 0.13</td>
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<td>1.51 ± 0.06</td>
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<td>N140304</td>
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<td>2.773</td>
<td>182</td>
<td>2.06 ± 0.19</td>
<td>1.96 ± 0.13</td>
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<td>2.25 ± 0.22</td>
<td>2.22 ± 0.14</td>
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<td>2.304</td>
<td>185</td>
<td>1.75 ± 0.14</td>
<td>1.75 ± 0.09</td>
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</table>

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conduction-limited radial temperature profile. In fact, \( T_{\text{in}}(\text{DT}) \) and \( T_{\text{in}}(\text{DD}) \) can also differ owing to a number of non-ideal factors such as scattering differences\(^a\) and Doppler motion spreading of the temporal signal registered by the NToF diagnostic if the fusion region is undergoing particular vortex\(^b\) or shearing motions. If \( T_{\text{in}}(\text{DT}) \) and \( T_{\text{in}}(\text{DD}) \) differ owing to motion in the fusion region, then mathematically we expect \( T_{\text{in}}(\text{DD}) \leq T_{\text{in}}(\text{DT}) \). As can be observed in Fig. 2 (bottom frames), as implosion velocity is increased in our experiments \( T_{\text{in}}(\text{DT}) \) and \( T_{\text{in}}(\text{DD}) \) do indeed differ by as much as 1.4 keV. One interpretation of this temperature difference is that it is an indication of some probable vortical or shearing fluid motions in the DT plasma, but if one simply applies the formula\(^a\), \( T_{\text{in}} = 5T_{\text{sn}}(\text{DD}) - 4T_{\text{in}}(\text{DT}) \), unphysically low temperatures (that is, a contradiction) are obtained. Some researchers would also propose kinetic effects as being responsible for the observed difference in \( T_{\text{in}}(\text{DT}) \) and \( T_{\text{in}}(\text{DD}) \), but estimation of the Knudsen number in our implosions’ hotspots indicates that kinetic effects should be quite small. It is likely that flows over some region, but not necessarily all, of the hotspot plasma in combination with scattering effects, through a broken up shell as implied by activation diagnostics\(^b\), are the primary drivers for the observed ion temperature differences. The model that best tracks the trend of \( T_{\text{in}}(\text{DT}) \) and \( \rho R_{\text{sn}} \) (Fig. 2 lower right-hand side) as well as the \( P_{\text{sn}} \) (Fig. 1) is one where \( A_{\text{sn}} \sim v^4 \) and the observed \( T_{\text{sn}}(\text{DT}) \) is treated as a superposition of two distributions, a 1D implosion contribution and a flow contribution. The perforation area scaling as \( v^4 \) can be simply understood as the consequence of deceleration phase-break-up: from a free-fall assumption \( gd \sim v^2 \) (\( g \) being the effective gravity and \( d \) being a typical inward directed Rayleigh–Taylor spike amplitude) and a weakly nonlinear assumption \( d \sim \lambda \) (\( \lambda \) being a typical feature wavelength), one obtains \( A_{\text{sn}} \sim \lambda^4 \sim v^4 \). Collectively, diagnostics and models that best match the data imply a picture of NIF high convection implosions that are consistent with an implosion shell that is highly distorted and perforated.

In spite of implosions having non-ideal shape, the degree of alpha-particle self-heating in the implosions can be determined (as seen in Fig. 2). An iterative procedure can be used to match the dynamic model to the bang-time data (\( Y, \text{burn-averaged } T_{\text{sn}}, \text{and hotspot volume} \)) and inferred burn-averaged \( P_{\text{sn}} \) and \( \rho R_{\text{sn}} \) data to within error bars for a given experiment as is shown in Fig. 2.

**Figure 3** | The scaling of fusion yield with fuel kinetic energy. Without alpha-particle self-heating, fusion yield is expected to scale as a constant power of energy (blue curve). With alpha-particle self-heating, the fusion yield is expected to scale with an ever-increasing power of energy (red curve). High-foot implosion experiments have exhibited yield scaling with \( E^{-5.8} \) depending on which subset of the suite of data is examined\(^c\). All error bars, 1σ.

**Figure 4** | X-ray energy radiated by hotspots from a variety of implosion experiments. 1D transport modelling of radiated energy from low-foot (LF) implosions\(^d\) (blue points) that are designed to achieve high compressions, but are R-T unstable, high-foot (HF) implosions\(^e\) (green points) that are designed to be more resistant to R-T instability, and high-density carbon (HDC) ablator experiments\(^f\) (yellow points) is compared to the radiated energy calculated using the optically thin limit of bremsstrahlung X-rays. Perhaps fortuitously, the agreement between the detailed transport model and the simple bremsstrahlung model is quite good. CH, carbon–hydrogen (that is, plastic, ablator material).

Measurements such as the duration of the fusion burn (that is, ‘burn width, \( \tau \)’) is automatically matched through this procedure because the inferred data incorporate \( \tau \) by construction\(^g\). This procedure can be used to infer the thermodynamic state of the hotspot at the time of peak fuel velocity (because this information is the initial data for the differential equations above). Moreover, equations (1)–(5), or equivalently equations (1), (2) and (6) can then be solved again forwards in time with the \( Q_{\text{in}} \) term dropped thereby calculating the time-dependent and burn-averaged properties of an equivalent implosion without any alpha-particle self-heating. Thus, we arrive at a method for determining the impact of alpha-particle self-heating on an individual implosion experiment on a case-by-case basis. The results can be compared (Table 1) with a correspondence between yield amplification \( (Y_{\text{α}}/Y_{\text{no-α}}) \) and measured yield and down-scatter ratio\(^h\) (the ratio of the number of neutrons measured in the energy range from 10 to 12 MeV over the number of neutrons measured in the energy range from 13 to 15 MeV) that was arrived at by a fit to a large database of simulated implosions\(^i\) as an alternative method for determining alpha-heating.

For a given ablator mass efficiency, with the thermodynamic properties of a given implosion experiment determined from the above procedure, we can then vary the amount of kinetic energy, \( E_k = (1/2) m_{\text{fuel}} v_{\text{fuel}}^2 \) in the dynamic model to obtain the scaling of fusion yield with and without alpha-particle self-heating (Fig. 3). As can be seen in Fig. 3, as the fusion fuel acquires higher levels of energy, the fusion yield responds to the fuel energy with an ever-increasing exponent, \( Y \sim E^A \), where \( A \geq 3 \), with \( A = 3 \) being the case of zero alpha-particle self-heating (for example, ref. 36). For \( A > 5.1 \), the yield multiplication due to alpha-particle self-heating doubles. This scaling of fusion yield with energy (or equivalently implosion velocity) allows us to determine the degree of alpha-particle self-heating for a suite of implosion experiments as an alternative method to the case-by-case determination. It has
been observed that the fusion yield scales with delivered laser energy, $E_{\text{laser}}$, as $Y \sim E_{\text{laser}}^\eta$ for the suite of high-foot experiments, shots N130501–N140819 (where on the NIF each ‘shot’ is labelled with a year-month-day format YYYYMMDD). Excluding shots whose fusion yields are below $1 \times 10^{15}$ neutrons from the data set, a scaling of $Y \sim E_{\text{laser}}^\eta$, is found. Furthermore, excluding all shots whose fusion yields are below $5 \times 10^{14}$ neutrons from the data set, a scaling of $Y \sim E_{\text{laser}}^\eta$ is found. It is expected that $E_{\text{laser}}$ is related to $E_{\text{laser}}$ through a series of efficiency factors, $E_{\text{p}} = \eta_{\text{ablator}} \eta_{\text{hohlraum}} \eta_{\text{laser}} E_{\text{laser}}$, where $\eta_{\text{ablator}}$ is the efficiency of conversion of laser energy to Planckian X-ray power at fixed energy (N140120 versus N140304); the effect of implosion shape improvement from tests of repeatability (N131219 versus N140225) as well as tests of ablator thickness with increasing laser drive: 175 $\mu$m ablator ‘T-1’ (N131219, N140225, N140311 and N140520) and 165-$\mu$m-thick ablators ‘T-1.5’ (N140707 and N140819). Some trends, such as increasing fusion performance with increasing implosion kinetic energy, fit expectations, whereas others, such as the null result with increasing laser power at fixed energy, contradict expectations.

As the high-foot implosion is used to probe the envelope parameter space of different drive and capsule conditions is probed. We have studied the response to increasing laser energy (shots N130812–N131119); the effect of implosion shape improvement through changes in hohlraum geometry or lower helium gas fill, as well as increasing time-dependent low-mode asymmetries exist in the implosions to higher levels of compression. The lowest-mode asymmetries are driven by a non-uniform X-ray illumination of the capsule by the hohlraum drive, whereas higher mode, but more localized, asymmetries/instabilities can be caused by engineering features such as the ‘tent’ diaphragm structure that holds the capsule in the centre of the hohlraum. Other engineering features such as the tube used to fill the capsule with DT are also a concern. Laser-plasma interactions that generate hot electrons (the presence of which is measured in our experiments) that preheat the DT fuel are also a potential performance degradation mechanism and may also be responsible for non-symmetric features on the implosion.

In the upcoming year, our programme will turn its attention to testing new hohlraums with increased diameters as compared with the capsule diameter (increased ‘case-to-capsule’ ratio). Either through changes in hohlraum geometry or lower helium gas fill, these new hohlraums should minimize hot electrons and create a more isotropic X-ray environment around our implosion using our well-characterized implosion as an integrated diagnostic of whether success has been achieved or not. Coupled to these integrated implosion experiments, a dedicated science team will be working to better measure and characterize the hohlraum plasma environment to better constrain simulations. Collaborative teams will continue working towards assessing the efficacy and trade-offs of alternative ablator materials as well as further maximizing instability control.

### Methods

Methods and any associated references are available in the online version of the paper.

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### References


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O.A.H. high-foot (HF) team co-lead dynamic model development and synthesis; D.A.C. HF team co-lead hohlraum drive and symmetry; D.T.C. DT shots (experiments) co-RI (responsible individual); E.L.D. 1DConA (velocity measurement) Shot RI, re-emit (X-ray re-emission experiment) Shot RI and data analysis and hot-electron analysis; T.R.D. 1D design physics and scoping; T.D. DT Shot RI and hard X-ray imaging analysis; S.H. DT ice layer characterization and instability growth-factor calculations; D.E.H. integrated hohlraum–capsule pulse-shape design physics and integrated post-shot modelling; L.F.R.H. keyhole (shock wave timing) shot pulse-shape design and post-shot modelling; O.I. hohlraum model design and development; A.L.K. integrated post-shot modelling and asymmetry analysis; S.L. keyhole Shot RI, T.M. DT Shot RI and hotspot shape analysis; A.G.M. capsule X-ray yield, data analysis tools, and 1DConA co-RI; J.L.M. hohlraum model development and re-emitter design; J.M. hohlraum and backscatter physics experiments; A.P. DT Shot co-RI, re-emit Shot RI and analysis, and hotspot shape analysis; H.-S.P. DT Shot RI; F.K.P. post-shot data analysis and hotspot model energy, pressure, and alpha-heating analysis; I.E.R. Synacman (hotspot symmetry measurement) Shot RI and backscatter analysis; H.F.R. keyhole platform design and hot-electron studies; J.S.R. hohlraum experiments; J.D.S. 1D post-shot modelling; B.K.S. development model database for alpha-heating analysis and NToF data analysis; F.T.S. hotspot, dynamic model development, and fit of Q_cal to SESAME database; R.T. 1DConA shot co-RI, data analysis and unfold of 2DConA data; F.A. FFLEX (hot-electron) data analysis; L.R.B. time-resolved hotspot shape X-ray measurement; R.B. FNADS (nuclear activation) spatial analysis; E.B. NToF data analysis; D.K.B. 2DConA (ablator shape) platform development; J.C. NToF data analysis; P.M.C. keyhole VISAR data analysis; C.C. 3D hotspot model analysis; J.A.C. GRH (gamma reaction history); R.D.S. DT ice layer cryogenics; D.E. south-pole bang time data analysis; M.J. Program Director; D.F. NIS (neutron imaging system) LLNL RS (responsible scientist); M.A.B.G. 2DConA Shot RI; A.H. target fabrication engineering; R.H. NToF data analysis; H.H. GRH data analysis; M.H. FFLEX data synthesis; D.H. target engineering; J.L.K. Synacman Shot RI and Dante (low-resolution X-ray temperature measurement) analysis; R.K. DT ice layer cryogenics and cryo-team science lead; G.K. X-ray imaging and analysis; G.G. fields and performs data analysis for the neutron imaging time-of-flight system; I.E.F. 2DConA data analysis; J.E. MRS (magnetic recoil spectrometer) diagnostic analysis; N.I. X-ray image data analysis; M.G.J. MRS diagnostic analysis; S.E.K. X-ray image analysis; J.K. nuclear data analysis; T.K. DT fuelling and tritium facility lead; O.L. fuel velocity inference; F.M. NIS LANL RS and performs data reduction, analysis, and error determination; P.M. hohlraum cross-bean energy transfer model and analysis; A.M. Dante diagnostic RS; S.R.N. 2DConA Shot co-RI, DIXI X-ray data analysis; A.N. target fabrication engineering; T.P. cryogenics and DT fuel team; R.R.B. 2DConA data analysis; D.S. GRH; M.S. SXR X-ray imaging analysis; D.S. spectral radio-chemistry data analysis; D.S. backscatter analysis; R.P.I.T. 2DConA platform design; A.W. high energy density program lead; K.W. Dante diagnostic RS; C.W. NIS diagnostic RI; F.V. develops algorithms to extract source information from NIS coded aperture; C.Y. FNADS (flange nuclear activation diagnostic system) analysis.

Additional information
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Competing financial interests
The authors declare no competing financial interests.
Methods

Justification for the acceptability of the optically thin limit of the bremsstrahlung X-ray cooling power is given. The scaling with temperature of the fusion reaction rate over different temperature regimes is shown. A partial set of analytic solutions to the dynamic model equations of this paper is given in the limit of balanced alpha-heating and X-ray losses.

Radiation losses: optical thin limit versus line radiation model. In Fig. 4, the X-ray energy radiated from the hotspot using the measured temperature, volume and inferred density for a variety of NIF implosions is compared under two different assumptions: using a detailed 1D transport model with a radial density profile and detailed configuration accounting opacities (ordinate) and the expression for bremsstrahlung losses in the optically thin limit, $Q_{\text{brems}}$, of the text (abscissa).

DT fusion reaction-rate scalings. Useful power-law, in temperature $T$, approximations to the DT reaction rate (in cm$^{-3}$ s$^{-1}$; ref. 40) are:

$$\langle \sigma v \rangle = 1.66 \times 10^{-20} T^{1.1} \pm 9\%, \quad 2 \leq T \leq 4$$

$$\langle \sigma v \rangle = 2.68 \times 10^{-20} T^{1.1} \pm 13\%, \quad 3 \leq T \leq 5$$

$$\langle \sigma v \rangle = 4.15 \times 10^{-20} T^{1.4} \pm 3\%, \quad 4 \leq T \leq 6$$

$$\langle \sigma v \rangle = 1.48 \times 10^{-19} T^{1.5} \pm 5\%, \quad 6 \leq T \leq 9$$

Hotspot dynamic equations in the adiabatic implosion limit. With $P_0$ and $R_0$ being the hotspot pressure and radius at peak velocity, $v_0$, at $t = 0$, the adiabatic compression condition ($P_0 R^2 = P_R R_0^2 = \text{const.}$, when the right-hand side of equation (6) is negligible) allows a simple solution to equation (1). Namely,

$$R(t) = \sqrt{R_{\text{min}}^2 + \frac{4\pi P_0 R_0^2}{\epsilon m_{\text{H}} c^2 R_{\text{min}}^2} (t - t_{\text{min}})^2}$$

$$\dot{R}(t) = \frac{1}{R(t)} \left( \frac{4\pi P_0 R_0^2}{\epsilon m_{\text{H}} c^2} - \frac{1}{R(t)^2} \right)$$

$$R_{\text{min}} = \frac{R_0}{1 + \frac{\epsilon m_{\text{H}} c^2 v_0^2}{4\pi P_0 R_0^2}} \approx \frac{4\pi P_0 R_0^2}{\epsilon m_{\text{H}} c^2 v_0^2} E_{\text{th}}^{-1/2}$$

$$t_{\text{min}} = \frac{v_0 R_0}{\dot{R}(t)} \approx R_0 / v_0$$

where $R_{\text{min}}$ is the minimum implosion radius and $t_{\text{min}}$ is the time between peak velocity and minimum radius. We are generally interested in the case where the kinetic energy of the shell at peak velocity considerably exceeds the hotspot internal energy, $2\pi P_0 R_0^2$, hence the approximate solutions above. The importance of the ratio of shell kinetic energy to hotspot internal energy has been noted previously. We note the peak stagnation pressure is achieved at $R_{\text{min}}$, so $P_{\text{stag}} = P_0 (R_0 / R_{\text{min}})^3 \sim E_{\text{th}}^{1/2}$. In the ion temperature range of 3–5 keV, the fusion yield then scales as $Y \sim P_{\text{stag}}^{1/3} V_0 t_{\text{burn}} \sim E_{\text{th}}^{1/3} V_0 t_{\text{burn}}$, where $t_{\text{burn}}$ is the burn duration of the implosion. In equation (5) if one drops the bremsstrahlung and mass loss terms, and then approximates $dT/dt \sim -T_0 / R_{\text{min}}$, the relation $T \sim E_{\text{th}}^{1/3} t_{\text{burn}}^{1/3}$ similar to ref. 18 is obtained. Thus, with no alpha-heating and no energy losses, the fusion yield will scale as $Y \sim E_{\text{th}}^{1/3} v_0^{1/3}$, because $V_0 t_{\text{burn}} \sim R_{\text{min}} / v_0$.

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